

Math Skills Laboratory

Lab 1 M S 2

MATH ACTIVITY

Substituting in Formulas

MATH SKILLS LAB OBJECTIVES

When you complete this activity, you should be able to do the following:

- 1. Given two of three quantities in an equation, solve the equation for the third quantity.*
- 2. Substitute numerical values in equations for density and fluid pressure, and solve the equation for the unknown quantity.*

LEARNING PATH

- 1. Read the Math Skills Lab. Give particular attention to the Math Skills Lab Objectives.*
- 2. Study Examples A and B.*
- 3. Work the problems.*

ACTIVITY

Substituting in Formulas

MATERIALS

For this activity, you'll need a hand calculator.

1. The mass density of any substance is equal to the mass of the substance divided by the volume of the substance. In equation form, density is given as follows:

$$\text{(In words) Density} = \frac{\text{Mass}}{\text{Volume}}$$

$$\text{(In symbols) } D = \frac{M}{V}$$

where: D = density

M = mass

V = volume

2. If the density of a substance is known, you can always find how much mass of that substance is contained in a given volume by rearranging the formula for density as follows:

(In words) Mass = Density \times Volume

(In symbols) $M = D \times V$

where: M = mass

D = density

V = volume

3. The pressure of any fluid is equal to the force acting on a given area divided by the area being acted on. In equation form, pressure is given as follows:

(In words) Pressure = $\frac{\text{Force}}{\text{Area}}$

(In symbols) $p = \frac{F}{A}$

where: p = pressure

F = force

A = area

4. Pressure of fluid at some depth in a tank is equal to the weight density of the fluid times the height of the fluid above the point where the pressure is measured.

(In words)

Pressure = Weight Density \times Height

(In symbols) $p = \rho_w h$

where: p = pressure

ρ_w = weight density

h = height (or depth)

5. Total pressure equals the sum of atmospheric pressure and gage pressure.

(In words)

Total Pressure = Atmospheric Pressure +
Gage Pressure

(In symbols) $p_{\text{tot}} = p_{\text{atm}} + p_g$

SOLVED EXAMPLES

Study the examples that follow. Each example shows how to calculate a certain unknown quantity by substitution in a known formula.

Example A: Calculating Density

Given: A volume of three cubic feet of sea water weighs 192 pounds.

Find: The weight density of sea water.

Solution: Step 1: Write down the formula for *weight density* in symbol form.

$$\rho_w = \frac{w}{V}$$

Step 2: Identify what is "given" and what needs to be "found."

Given: Weight (w) = 192 lb

Volume (V) = 3 cubic feet = 3 ft³

Find: Weight density (ρ_w)

Step 3: Substitute "given" values for w and V in the formula, including both the numerical value and units.

$$\rho_w = \frac{w}{V} = \frac{192 \text{ lb}}{3 \text{ ft}^3}$$

Step 4: Use a calculator to perform the indicated division. Write out the answer, including both the numerical result and the units.

$$\rho_w = 64 \frac{\text{lb}}{\text{ft}^3}$$

Conclusion: The weight density of sea water has been calculated to be 64 pounds per cubic foot. Note that the correct answer includes both a number (64) and units (lb/ft³).

Example B: Calculating Mass

Given: Antifreeze (ethylene glycol) has a density of 1.125 gm/cm^3 at the freezing temperature of water.

Find: The mass of one liter of antifreeze. (One liter = 1000 cm^3 .)

Solution: Step 1: Write down the formula for mass in symbol form. $M = D \times V$

Step 2: Identify what is **given** and what is to be **found**.

Given: Density (D) = 1.125 gm/cm^3

Volume (V) = 1000 cm^3

Find: Mass (M)

Step 3: Substitute given values for D and V in the formula, including numbers and units.

$$M = D \times V$$

$$M = 1.125 \frac{\text{gm}}{\text{cm}^3} \times 1000 \text{ cm}^3$$

Step 4: Use your calculator to complete the indicated multiplication. Write out numbers and units.

$$M = 1125 \frac{\text{gm} \cdot \cancel{\text{cm}^3}}{\cancel{\text{cm}^3}} \quad (\text{Cancel identical units.})$$

$$M = 1125 \text{ gm}$$

Conclusion: The mass of one liter of ethylene glycol at 32°F is 1125 gm or 1.125 kg.

Note: The units $\frac{\text{gm} \cdot \text{cm}^3}{\text{cm}^3}$ are correct, but can be simplified by canceling the cm^3 in the numerator with cm^3 in the denominator, leaving the unit gm . Since gm is a mass unit, and the calculation was to determine a mass, the units come out correctly.

PRACTICE EXERCISES

Problem 1: Mercury is used as a liquid in thermometers. A volume of five cubic centimeters (5 cm^3) of mercury has a mass of 68 grams (68 gm). What is the density of mercury in gm/cm^3 ?

(Use the formula, $D = \frac{M}{V}$.)

Problem 2: Oak wood floats in water. A 400-lb chunk of oak wood occupies a volume of about 8 cubic feet (8 ft^3). What is the weight density of oak wood in lb/ft^3 ?

(Use the formula, $\rho_w = \frac{W}{V}$.)

Problem 3: Gold is a heavy metal. It has a density of 19.3 gm/cm^3 . What is the mass of 10 cubic centimeters (10 cm^3) of gold?

(Use the formula, $M = D \times V$.)

Problem 4: Oil floats on water. Oil has a density of 0.9 gm/cm^3 . What is the mass of one liter (1000 cm^3) of oil?

(Use the formula, $M = D \times V$.)

Problem 5: Air is stored under pressure in a tank. The air exerts a total force of 5000 lb against the tank wall. The total surface area of the tank wall is 500 in². What is the tank pressure?

(Use the formula, $p = \frac{F}{A}$.)

Problem 6: What is the force exerted by a pressure of 480 lb/in² on a hydraulic piston that has a surface area of 6 in²?

(Use the formula, $F = p \times A$.)

Problem 7: Find the pressure of air at the bottom of a column of air 30,000 ft high with a weight density of 0.056 lb/ft³.

(Use the formula, $p = \rho_w \times h$.)

Problem 8: At sea level, atmospheric pressure is 14.7 lb/in². What is the total pressure of air in an inner tube that has a gage pressure of 40 lb/in²?

(Use the formula, $p_{\text{tot}} = p_{\text{atm}} + p_g$.)